



Workshop Aims

Correlation  $\neq$   
Causation

Causal  
Framework

Confounders

Colliders

Mediators

Recap

## Quantitative Social Research II

### Workshop 3: Path Analysis and the Causal Framework

Jose Pina-Sánchez



## Workshop Aims: Recap

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Recap

- Last week we contrasted two model building strategies
  - data driven (inductive, exploratory, seeking to predict)
  - theory driven (deductive, confirmatory, seeking to explain)
- Question: Why is the former not good at explaining?



## Workshop Aims: Recap

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Recap

- Last week we contrasted two model building strategies
  - data driven (inductive, exploratory, seeking to predict)
  - theory driven (deductive, confirmatory, seeking to explain)
- Question: Why is the former not good at explaining?
  - over-fitted models leading to problems of multicollinearity, etc.
  - arbitrary selection of variables, p-hacking
- We need to pre-identify the right variables to be included in the model if we want to
  - test hypotheses
  - describe causal mechanisms
- To do so (to identify the right explanatory variables) we need theory
  - and a few important concepts from the causal framework

# Workshop Aims

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- The causal framework offers a systematic approach to interpret the theoretical role of different variables
  - cause and effect
  - but also confounders, colliders, mediators and more
- We should be careful as to how/where they should be included
  - and how they are related to each other
- We'll present these concepts and put them in practice using data from
  - The Labour Force Survey
  - Pathways to Desistance



# Correlation $\neq$ Causation

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- Correlation does not imply causation, lookout for *spurious* correlations



# Correlation $\neq$ Causation

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- Correlation does not imply causation, lookout for *spurious* correlations
- Two given variables ( $X$  and  $Y$ ) might be correlated for different reasons:



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  - $X \rightarrow Y$ , the expected causal path, if so, correlation = causation



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- Correlation does not imply causation, lookout for *spurious* correlations
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  - $X \rightarrow Y$ , the expected causal path, if so, correlation = causation
  - $Y \rightarrow X$ , the causal path works in reverse
  - $Z \rightarrow X, Y$ , a third variable (a *confounder*) might be causing both the alleged cause and effect



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  - $X \rightarrow Y$ , the expected causal path, if so, correlation = causation
  - $Y \rightarrow X$ , the causal path works in reverse
  - $Z \rightarrow X, Y$ , a third variable (a *confounder*) might be causing both the alleged cause and effect
  - also, due to problems of data quality (e.g. measurement error, non-response) or research design (e.g. coverage error)



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## Experimental, Longitudinal and Cross-Sectional Data

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# Experimental, Longitudinal and Cross-Sectional Data

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  - we compare subjects in similar (randomised) groups before and after we intervene in one of those groups
  - no confounders, the two groups are identical because subjects are allocated to the ‘intervention’ or ‘control’ group at random
  - no reverse causality, we control the timing of the intervention and compare results from before and after
  - hard to carry out in the social sciences

Question: do you know why?

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## Experimental, Longitudinal and Cross-Sectional Data

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- We can rule out the presence of reverse causality and confounding effects using experiments
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Question: do you know why?
- We can explore reverse causal paths using longitudinal data
  - the problem of confounding effects is still present though
- When we have cross-sectional data we have to rely on a series of assumptions
  - the causal framework is just a tool to help us formalise those assumptions

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Recap

- Use theory to represent the expected causal relationships between our variables before we run our models
- Create a causal diagram (a DAG) where the variables involved are considered either
  - parents (cause, explanatory variables)
  - descendants (effect, outcome variables)
- But also consider additional roles of those variables in more complex causal relationships
  - confounders
  - colliders
  - mediators

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- Variables that cause both the outcome and an explanatory variable
  - higher salaries ( $Y$ ) paid to older ( $X$ ) workers are confounded by experience ( $Z$ )
  - longer sentences ( $Y$ ) for male ( $X$ ) offenders are confounded by their rehabilitation potential ( $Z$ )
  - shorter sentences ( $Y$ ) for remorseful offenders ( $X$ ) are confounded by legal representation ( $Z$ )
  - higher number of car crashes ( $Y$ ) are recorded for taller drivers ( $X$ ), which is confounded by their sex ( $Z$ )
- We should include (control for) all potential confounders
  - otherwise the relationship between  $X$  and  $Y$  will be biased

# Modelling Confounders

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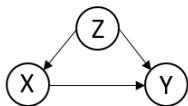
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## Causal relationship

(e.g. shorter sentences,  $Y$ , for remorseful offenders,  $X$ , are confounded by legal representation,  $Z$ )





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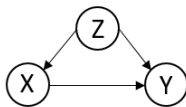
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Recap

# Modelling Confounders

## Causal relationship

(e.g. shorter sentences,  $Y$ , for remorseful offenders,  $X$ , are confounded by legal representation,  $Z$ )



## Bad model

$$Y = \alpha + \beta X + e$$

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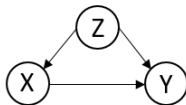
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Recap

# Modelling Confounders

## Causal relationship

(e.g. shorter sentences,  $Y$ , for remorseful offenders,  $X$ , are confounded by legal representation,  $Z$ )



Bad model

$$Y = \alpha + \beta X + e$$

Good model

$$Y = \alpha + \beta_1 X + \beta_2 Z + e$$

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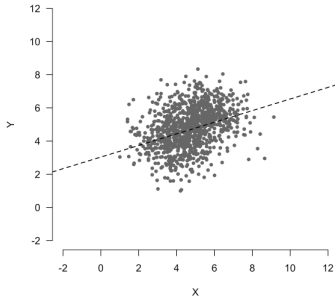
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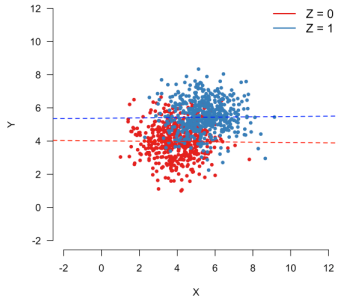
## Confounder Effect

(e.g. taller drivers have more car crashes)

Marginal Dependence between X and Y



Conditional Independence between X and Y given Z

Source: [Fabian Dablander](#)

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Recap

- Assumptions in the linear regression model ( $Y = \alpha + \beta_k X_k + e$ ):
  - normality: residuals are normally distributed
  - homoskedasticity: the variance of the residuals is constant
  - independence: residuals are independent of each other
  - no multicollinearity
  - perfectly measured variables
  - no missing data (other than missing at random)
  - **no unobserved confounders**: we control for all common causes of  $X_1$  and  $Y$
  - no reverse causality:  $Y$  does not cause  $X_1$
  - linearity: the effect of  $X_1$  on  $Y$  is the same across the range of  $X_1$



## Confounder Effect: Mathematically

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Recap

- Variability in the dependent variable that is not controlled for the explanatory variables included in the model is captured by the error term
  - true model:  $Y = \beta_0 + \beta_1 X + \beta_2 Z + e$
  - our model:  $Y = \beta_0 + \beta_1 X + e^*$
  - then our residuals:  $e^* = e + \beta_2 Z$

## Confounder Effect: Mathematically

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- Variability in the dependent variable that is not controlled for the explanatory variables included in the model is captured by the error term
  - true model:  $Y = \beta_0 + \beta_1 X + \beta_2 Z + e$
  - our model:  $Y = \beta_0 + \beta_1 X + e^*$
  - then our residuals:  $e^* = e + \beta_2 Z$
- If  $Z$  is a confounder (causing  $Y$  but also associated to  $X$ )
- Then  $\hat{\beta}_1^*$ , the estimated effect of  $X$  on  $Y$  is biased

$$- \hat{\beta}_1^* = \overbrace{\frac{Cov(Y, X)}{Var(X)}}^{\hat{\beta}_1} + \overbrace{\beta_2 \frac{Cov(Z, X)}{Var(X)}}^{bias}$$

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- Confounders which are not a cause but an effect of the outcome variable
  - the duration of a custodial sentence ( $Y$ ) will determine whether the sentence is reviewed by the Parole Board ( $Z$ ), which is also determined by the seriousness of the case ( $X$ )
  - being attractive ( $X$ ) and being intelligent ( $Y$ ) are two unrelated traits, but they are both -probably- inversely related for those in a couple ( $Z$ ) (e.g. Megan Fox voted the worst and most attractive actress)
  - obesity ( $X$ ) is negatively related to life expectancy ( $Y$ ) but positively amongst people with diabetes ( $Z$ )
- We should not condition on any colliders (or their descendants)
  - otherwise the relationship between  $X$  and  $Y$  will be biased

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Causal relationship







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Bad model

$$Y = \alpha + \beta_1 X + \beta_2 Z + e$$



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Bad model

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Good model

$$Y = \alpha + \beta X + e$$

## Collider Bias

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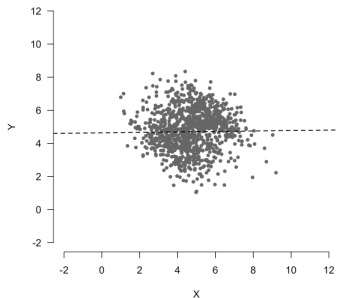
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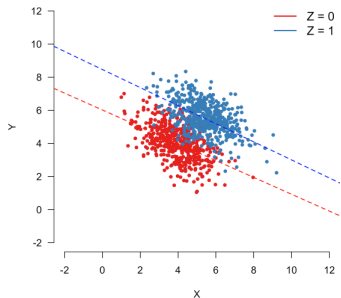
Recap

(e.g. beauty and talent are unrelated, except for movie starts)

Marginal Independence between X and Y



Conditional Dependence between X and Y given Z

Source: [Fabian Dablander](#)



# Mediators

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Recap

- A variable  $Z$  through which  $X$  has a causal effect on  $Y$ 
  - *full mediation*,  $X$  only has an indirect effect on  $Y$ , as in  $X \rightarrow Z \rightarrow Y$
  - *partial mediation*, when  $X$  also has a direct effect on  $Y$
  - e.g. grades  $\rightarrow$  happiness, mediated by self-esteem
  - Question: are there mediating paths in the gender gap model?

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- A variable  $Z$  through which  $X$  has a causal effect on  $Y$ 
  - *full mediation*,  $X$  only has an indirect effect on  $Y$ , as in  $X \rightarrow Z \rightarrow Y$
  - *partial mediation*, when  $X$  also has a direct effect on  $Y$
  - e.g. grades  $\rightarrow$  happiness, mediated by self-esteem
  - Question: are there mediating paths in the gender gap model?
- If we want to disentangle the different (*direct* and *indirect*) effects of  $X$  on  $Y$ ,
  - we need to specify the potential *mediating* (*indirect*) effects
  - otherwise we will be estimating its *total* effect (i.e. its *direct* + *indirect* effect) if we do not control for  $Z$ , and only the direct effect if we do



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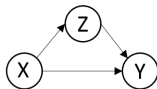
**Mediators**

Recap

# Modelling Mediators

## Causal relationship (partial mediation)

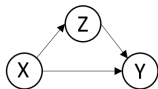
(e.g. the gender gap in academia with  $Z$  being academic ranking)



## Modelling Mediators

### Causal relationship (partial mediation)

(e.g. the gender gap in academia with  $Z$  being academic ranking)



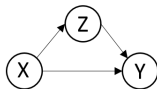
Bad model (we only estimate the direct effect, the indirect effect is controlled for)

$$Y = \alpha + \beta_1 X + \beta_2 Z + e$$

## Modelling Mediators

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(e.g. the gender gap in academia with  $Z$  being academic ranking)



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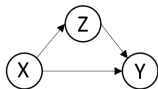
Better model (we estimate the total effect, although the direct and indirect effects are not disentangled)

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## Modelling Mediators

## Causal relationship (partial mediation)

(e.g. the gender gap in academia with  $Z$  being academic ranking)

Bad model (we only estimate the direct effect, the indirect effect is controlled for)

$$Y = \alpha + \beta_1 X + \beta_2 Z + e$$

Better model (we estimate the total effect, although the direct and indirect effects are not disentangled)

$$Y = \alpha + \beta_1 X + e$$

Even better model (we estimate the direct effect, then the indirect effect through a second model)

$$Z = \alpha + \beta_1 X + e$$

$$Y = \alpha + \beta_2 X + \beta_3 Z + e$$

$$\text{Total Effect}_X = \overbrace{\beta_1 \beta_3}^{\text{Indirect Effect}} + \overbrace{\beta_2}^{\text{Direct Effect}}$$

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Recap

- We have learnt useful model building strategies when we seek to *explain*
  - to approximate the causal relationship between two variables more accurately we need to control for confounding factors
  - introducing all the variables in a model in order to ‘control’ for them is not the right approach
  - rather we need to think carefully about the underlying causal relationships
  - if interested in disentangling direct and indirect effects you might want to consider potential mediating effects
- To learn more read:
  - van der Weele (2011) ‘Causal diagrams for empirical legal research: A methodology for identifying causation, avoiding bias and interpreting results’
- In Workshop 8 we will learn how to use longitudinal data to model reverse causal effects